

Lutz Frommberger

Qualitative Spatial Abstraction in Reinforcement Learning

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Foreword

Teaching and learning are difficult tasks not only when people are involved but also with regard to computer programs and machines: When the teaching/learning units are too small, we cannot express sufficient context to teach a differentiated lesson; when they are too large, the complexity of the learning task can increase dramatically such that it will take forever to teach and learn a lesson. Thus, the question arises, how we can teach and learn complex concepts and strategies, or more specifically: How can the lesson be structured and scaled such that efficient and effective learning can be achieved?

Reinforcement learning has developed as a successful learning approach for domains that are not fully understood and that are too complex to be described in closed form. However, reinforcement learning does not scale well to large and continuous problems; furthermore, knowledge acquired in one environment cannot be transferred to new environments. Although this latter phenomenon also has been observed in human learning situations to a certain extent, it is desirable to generalize suitable insights for application also in new situations.

In this book, Lutz Frommberger investigates whether deficiencies of reinforcement learning can be overcome by suitable abstraction methods. He discusses various forms of spatial abstraction, in particular qualitative abstraction, a form of representing knowledge that has been thoroughly investigated and successfully applied in spatial cognition research. With his approach, Lutz Frommberger exploits spatial structures and structural similarity to support the learning process by abstracting from less important features and stressing the essential ones. The author demonstrates his learning approach and the transferability of knowledge by having his system learn in a virtual robot simulation system and consequently transferring the acquired knowledge to a physical robot.

Lutz Frommberger's approach is influenced by findings from cognitive science. In this book, he focuses on the role of knowledge representation for the learning process: Not only is it important to consider *what* is represented, but also *how* it is represented. It is the appropriate representation of an agent's perception that enables generalization in the learning task and that allows for reusing learned policies in new contexts—without additional effort. Thus, the choice of spatial representation

for the agent's state space is of critical importance; it must be well considered by the designer of the learning system. This book provides valuable help to support this design process.

Bremen, September 2010

Christian Freksa

Preface

Abstraction is one of the key capabilities of human cognition. It enables us to conceptualize the surrounding world, build categories, and derive reactions from these categories to cope with different situations. Complex and overly detailed circumstances can be reduced to much simpler concepts, and not until then does it become feasible to deliberate about conclusions to draw and actions to take.

Such capabilities, which come easily to a human being, can still be a big challenge for an artificial agent: In the past years of research I investigated how to employ such human concepts in a learning machine. In particular, my research focused on utilizing spatial abstraction techniques in agent control, using the machine learning paradigm of reinforcement learning. This led to results published in journals and conference proceedings over the years that are now integrated and significantly extended to a comprehensive study on spatial abstraction in reinforcement learning in this book. It spans the whole range from formal aspects to empirical results.

Reinforcement learning allows us to learn successful strategies in domains that are too complex to be described in a closed model or in cases where the system dynamics are only partially known. It has been shown to be effectively applicable to a large number of tasks and applications. However, reinforcement learning in its “pure” form shows severe limitations in practical use. In particular, it does not scale well to large and continuous problems, and it does not allow for reuse of already gained knowledge within the learning task or in new tasks in unknown environments. Spatial abstraction is an appropriate way to tackle these problems.

When regarding the nature of abstraction, I believe that only a consistent formalization of abstraction allows for a thorough investigation of its properties and effects. Thus, I present formal definitions that distinguish between three different facets of abstraction: aspectualization, coarsening, and conceptual classification. Based on these definitions it can be shown that aspectualization and coarsening can be utilized to achieve the same effect. Hence, the process of aspectualization is to be preferred when using spatial abstraction in agent control processes, as it is computationally simple and its features are easily accessible. This allows for coping even with high-dimensional state spaces. The property of a representation being aspectualizable turns out to be central for agent control.

In order to use abstraction to control artificial agents, I argue for an action-centered view on abstraction that concentrates on the decisions being drawn at certain states. I derive criteria for efficient abstraction in agent control tasks and show that these criteria can most satisfactorily be matched by the use of qualitative representations, especially when they model important aspects in the state space such that they can be accessed by aspectualization.

In sequential decision problems we can distinguish between goal-directed and generally sensible behavior. The corresponding spatial features form task space and structure space. As it is of special importance to describe structural elements of the state space explicitly in an abstract representation, I introduce the concept of structure space aspectualizable observation spaces. For this kind of state space, two methods are developed in this book: task space tile coding (TSTC) and a posteriori structure space transfer (APSST). They allow for reusing structural knowledge while learning to solve a task and also in different tasks in unknown environments. Furthermore, I introduce structure-induced task space aspectualization (SITSA), a mechanism for situation-dependent spatial abstraction based on knowledge gained from a structural analysis of learned policies in previous tasks.

We will study the effect of the proposed techniques on an instance of structure space aspectualizable state spaces, namely le-RLPR, an abstract spatial representation tailored for robot navigation in indoor environments. It describes the circular order of landmarks around the moving robot and the relative position of walls with regard to the agent's moving direction. Compared to coordinate-based metrical approaches, le-RLPR enables us to learn successful strategies for goal-directed navigation tasks considerably faster. Policies learned with le-RLPR also allow for generalization within the actual learning task as well as for transferring knowledge to new scenarios in unknown environments. As a final demonstration we will see that RLPR-based policies learned in a simulator can also be transferred to a real robotics system with little effort and allow for sensible navigation behavior of a robot in office environments.

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At this point I want to express my gratitude to several people who helped me during my work on this book.

First of all, I thank Christian Freksa for advising my doctoral thesis and giving me the opportunity to work in the Cognitive Systems research group at the University of Bremen. He brings together people from various scientific fields for interdisciplinary research. This provides an inspiring and productive atmosphere, and I am thankful that I was involved there for so many years. Christian has been always available when I needed advice. Often, his comments and ideas made me look at my work from a different point of view and thus broadened my mind.

Furthermore, I want to express my gratitude to Ramon López de Mántaras for his willingness to be a reviewer of my doctoral thesis and especially for his enthusiasm and his detailed and encouraging remarks on my work.

Particularly in the early stages of my research it had been important to receive encouraging feedback on the ideas I had. In particular, I thank Reinhard Moratz for initially supporting my approach. Furthermore, I thank Joachim Hertzberg, Frank Kirchner, Martin Lauer, George Konidakis, and Stefan Wölfl for inspiring and encouraging discussions that helped me to focus my work. Also, several anonymous reviewers provided substantial feedback on papers emerging from ongoing work on this book that I submitted to workshops, conferences, and journals.

Martin Riedmiller sparked my interest in reinforcement learning when I was a student at the University of Karlsruhe. I thank him for repeatedly giving me the opportunity to extensively discuss my work with him and his Neuroinformatics group at the University of Osnabrück. I acknowledge especially Stephan Timmer's valuable comments and hints regarding my approach.

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Bremen, September 2010

Lutz Frommberger

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Symbols

\mathcal{A}	Action space, 10
c_i	Sampled color view, 104
cert	Decision certainty for a state, 89
Conf	Decision confidence for a policy, 85
conf	Decision confidence for a state, 85
\mathcal{D}	Arbitrary domain, 45
E	Expected value (in statistics), 13
e	Eligibility trace, 18
H	Horizon, 11
h	Hash function, 76
\mathcal{I}	Initiation set for options, 31
I^K	Aspectualization index vector, 52
I^K	Inverse aspectualization index vector, 52
L^*	Set of all detected landmarks, 100
L_i	Sector for landmark selection, 100
l_{\max}	Maximum number of landmarks allowed in a sector, 101
\mathcal{O}	Observation space, 15
$\mathcal{O}_{\text{NDesc}}$	Set of non-decision structures, 90
\mathcal{O}_S	Structure space, 71
\mathcal{O}_T	Task space, 71
p^{\max}	Vector of maximum feature values, 79
p_i^{\max}	Maximum feature value of dimension i , 79
Q	Action-value function, 14
Q^*	Optimal action-value function, 19
Q_S	Structure space Q-function, 83
Q_T	Task space Q-function, 87
$q\pi^*$	π^* -preservation quota, 56
\mathcal{R}	RLPR grid, 110
R	Reward function, 12
\mathcal{S}	State space, 10
s	State, 10

ssd	Structure space descriptor, 72
T	State transition function, 12
tsd	Task space descriptor, 72
V	Value function, 13
V^*	Optimal value function, 13
α	Learning rate, 18
β_i	Landmark sample angle, 104
χ	Tiling function, 76
γ	Discount factor, 13
δ	Temporal difference error, 18
ε	Exploration probability, 17
ζ	Motion noise parameter, 124
Θ	SITSA abstraction function, 90
κ	Abstraction function, 45
λ	Trace decay parameter, 19
μ	Task/structure space weight, 87
ξ	SMDP waiting time parameter, 31
π	Policy, 11
π^*	Optimal policy, 11
π_S	Structure space policy, 72
ρ	Line detection distortion parameter, 140
σ	Landmark noise parameter, 139
τ	RLPR overlap status, 111
$\bar{\tau}$	RLPR overlap status (whole scene), 111
$\bar{\bar{\tau}}$	RLPR overlap status (whole scene, boolean), 111
τ'	RLPR adjacency status, 111
$\bar{\tau}'$	RLPR adjacency status (whole scene), 111
$\bar{\bar{\tau}'}$	RLPR adjacency status (whole scene, boolean), 111
ψ	Observation function, 15
ψ_S	Structure space observation function, 114
ψ_T	Task space observation function, 100
ω	Observation in an observation space, 15
$\bar{\omega}$	Structure space observation, 83
\perp	Empty symbol, 90
\equiv_2	modulo 2, 15
\sim	Similarity operator, 55

Acronyms

A-CMAC	Averager cerebellar model articulator controller
APSST	A posteriori structure space transfer
CMAC	Cerebellar model articulator controller
MDP	Markov decision process
QSR	Qualitative spatial reasoning
POMDP	Partially observable Markov decision process
RL	Reinforcement learning
RLPR	Relative line position representation
SDALS	Structural-decision-aware landmark selection
SITSA	Structure-induced task space aspectualization
SMDP	Semi-Markov decision process
TSTC	Task space tile coding

Chapter 1

Introduction

One of the most essential properties of a cognitive being is its ability to learn. Learning is the “process of acquiring modifications in existing knowledge, skills, habits, or tendencies through experience, practice, or exercise” ([Encyclopædia Britannica, 2007](#)). These modifications lead to a performance improvement of the cognitive being (also called *cognitive agent*) in the tasks it has to solve in its daily routines. Learning provides the agent with a preferably good adaptation of its behavior to the situations it is confronted with.

While most of the learning efforts of human beings and animals are achieved in the early years, learning is generally a life-long process. Perceived situations may change over time, and even the perception abilities themselves may change, and the dynamics of the agent may vary due to age or abrasion. These changes require continuous adaptations of the acquired strategies and behaviors over a longer period of time. It is desirable to find this ability also in artificial cognitive agents, for example, in autonomous robots.

1.1 Learning Machines

Much effort has been spent in the field of artificial intelligence (AI) to investigate methods for machine learning. This field of research spans two distinct paradigms. *Supervised learning* requires external knowledge given by an expert, who supervises the learning process. The learning agent is supposed to find a mapping between its input values and the desired output that is given by the expert. In contrast, *unsupervised learning* autonomously constructs a classification of the input without intervention from outside. Many types of machine learning approaches exist somewhere between supervised and unsupervised learning.

This book concentrates on one of the most influential machine learning techniques: the learning paradigm of *reinforcement learning* (RL) ([Sutton and Barto, 1998](#)). In RL, learning does not take place by teaching or supervision, but by interaction with a dynamic and uncertain environment. It can be seen as a form of